

chain-replication-acks^{13,45}

chain-replication-acks{i:l}

$$\begin{aligned}
& (es; Cmd; Rsp; isupdate; In; Out; Sys; Ack; f; g; Delta; Q) \\
\equiv_{\text{def}} & \text{fifo-antecedent}(es; Sys; f) \ \& \ \text{fifo-antecedent}(es; Ack; g) \\
& \ \& \ (\forall u: E(Sys). (f(u) = u) \iff (\uparrow(u \in_b In))) \\
& \ \& \ (E(In) \subseteq_r E(Sys)) \\
& \ \& \ (E(Out) \subseteq_r E(Sys)) \\
& \ \& \ (E(Out) \subseteq_r E(Ack)) \\
& \ \& \ (\forall e: E(In). (\neg(\uparrow(isupdate(In(e)))) \Rightarrow (\uparrow(e \in_b Out)))) \\
& \ \& \ (\forall e: E(Sys). (\neg(\uparrow(e \in_b In))) \Rightarrow (\text{loc}(f(e)) = \text{loc}(e)) \Rightarrow (\neg(\uparrow(e \in_b Out)))) \\
& \ \& \ \text{input-forwarding}\{i:l\} \\
& \ \ \ \ \ (es; Cmd; Sys; isupdate; In; f) \\
& \ \& \ (\exists chain: \{e: E \mid (\uparrow(e \in_b Sys)) \vee (\uparrow(e \in_b Ack))\} \rightarrow (\text{Id List})) \\
& \ \ \ \ \ (\text{chain-config}(es; \text{p-conditional}(Ack; Sys); chain) \\
& \ \ \ \ \ \& \ \text{chain-consistent}(f; chain) \\
& \ \ \ \ \ \& \ (\forall e: E(Ack). \\
& \ \ \ \ \ \ \ \ \ \ \ (\neg(\text{loc}(g(e)) = \text{loc}(e))) \\
& \ \ \ \ \ \ \ \ \ \ \ \Rightarrow (\text{adjacent}(\text{Id}; chain(e); \text{loc}(e); \text{loc}(g(e))) \\
& \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \& \ \text{adjacent}(\text{Id}; chain(g(e)); \text{loc}(e); \text{loc}(g(e)))))) \\
& \ \& \ (\forall e: E(Ack). (\text{loc}(g(e)) = \text{loc}(e)) \Rightarrow (\uparrow(e \in_b Out))) \\
& \ \& \ (\forall e: E(Ack). (\uparrow(e \in_b Out)) \Rightarrow (g(e) = e)) \\
& \ \& \ (\forall e: E(Ack). (\uparrow((g(e)) \in_b Out)) \Rightarrow \text{is-query}(In; isupdate; g(e)) \Rightarrow (g(e) = e)) \\
& \ \& \ (\forall e: E(Out). \\
& \ \ \ \ \ (\text{is-query}(In; isupdate; e) \\
& \ \ \ \ \ \Rightarrow (Out(e) = Q(\text{filter}(isupdate; \text{es-interface-history}(es; Sys; e), In(e)))) \\
& \ \ \ \ \ \& \ ((\neg \text{is-query}(In; isupdate; e)) \\
& \ \ \ \ \ \ \ \ \ \ \ \Rightarrow (Out(e) = Delta(\text{filter}(isupdate; \text{es-interface-history}(es; Sys; e)))))) \\
& \ \& \ (\forall e: E(Ack). \\
& \ \ \ \ \ Ack(e) = \text{if } e \in_b Out \text{ then } \|\text{filter}(isupdate; Sys(e))\| \text{ else } Ack(g(e)) \text{ fi})
\end{aligned}$$

clarification:

chain-replication-acks{i:l}

$$\begin{aligned}
& (es; Cmd; Rsp; isupdate; In; Out; Sys; Ack; f; g; Delta; Q) \\
\equiv_{\text{def}} & \text{fifo-antecedent}(es; Sys; f) \ \& \ \text{fifo-antecedent}(es; Ack; g) \\
& \ \& \ (\forall u: \text{es-E-interface}(es; Sys). (f(u) = u \in \text{es-E}(es)) \iff (\uparrow(u \in_b In))) \\
& \ \& \ (\text{es-E-interface}(es; In) \subseteq_r \text{es-E-interface}(es; Sys)) \\
& \ \& \ (\text{es-E-interface}(es; Out) \subseteq_r \text{es-E-interface}(es; Sys)) \\
& \ \& \ (\text{es-E-interface}(es; Out) \subseteq_r \text{es-E-interface}(es; Ack)) \\
& \ \& \ (\forall e: \text{es-E-interface}(es; In). (\neg(\uparrow(isupdate(In(e)))) \Rightarrow (\uparrow(e \in_b Out)))) \\
& \ \& \ (\forall e: \text{es-E-interface}(es; Sys). \\
& \ \ \ \ \ (\neg(\uparrow(e \in_b In))) \Rightarrow (\text{es-loc}(es; (f(e))) = \text{es-loc}(es; e) \in \text{Id}) \Rightarrow (\neg(\uparrow(e \in_b Out)))) \\
& \ \& \ \text{input-forwarding}\{i:l\}
\end{aligned}$$

$$\begin{aligned}
& (es; Cmd; Sys; isupdate; In; f) \\
& \& (\exists chain: \{e: es-E(es) \mid (\uparrow(e \in_b Sys)) \vee (\uparrow(e \in_b Ack))\} \rightarrow (Id \text{ List})) \\
& \quad (\text{chain-config}(es; p\text{-conditional}(Ack; Sys); chain) \\
& \quad \& \text{chain-consistent}(es; Sys; In; isupdate; Out; f; chain) \\
& \quad \& (\forall e: es-E\text{-interface}(es; Ack). \\
& \quad \quad (\neg(\text{es-loc}(es; (g(e))) = \text{es-loc}(es; e) \in Id)) \\
& \quad \quad \Rightarrow (\text{adjacent}(Id; chain(e); \text{es-loc}(es; e); \text{es-loc}(es; (g(e)))) \\
& \quad \quad \quad \& \text{adjacent}(Id; chain(g(e)); \text{es-loc}(es; e); \text{es-loc}(es; (g(e)))))) \\
& \& (\forall e: es-E\text{-interface}(es; Ack). \\
& \quad (\text{es-loc}(es; (g(e))) = \text{es-loc}(es; e) \in Id) \Rightarrow (\uparrow(e \in_b Out))) \\
& \& (\forall e: es-E\text{-interface}(es; Ack). (\uparrow(e \in_b Out)) \Rightarrow (g(e) = e \in es-E(es))) \\
& \& (\forall e: es-E\text{-interface}(es; Ack). \\
& \quad (\uparrow((g(e)) \in_b Out)) \Rightarrow \text{is-query}(In; isupdate; g(e)) \Rightarrow (g(e) = e \in es-E(es))) \\
& \& (\forall e: es-E\text{-interface}(es; Out). \\
& \quad (\text{is-query}(In; isupdate; e) \\
& \quad \Rightarrow (Out(e) = Q(\text{filter}(isupdate; \text{es-interface-history}(es; Sys; e)), In(e)) \in Rsp)) \\
& \quad \& ((\neg \text{is-query}(In; isupdate; e)) \\
& \quad \Rightarrow (Out(e) = \Delta(\text{filter}(isupdate; \text{es-interface-history}(es; Sys; e))) \in Rsp))) \\
& \& (\forall e: es-E\text{-interface}(es; Ack). \\
& \quad Ack(e) = \text{if } e \in_b Out \text{ then } \|\text{filter}(isupdate; Sys(e))\| \text{ else } Ack(g(e)) \text{ fi } \in \mathbb{Z}
\end{aligned}$$